

QUANTUM SIMULATION IN **OPTICAL SUPERLATTICE**

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LUDWIG-

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National Laboratory for Physical Sciences at Microscale

Quantum communication quantum computation

Information

Understanding physics for complex system

Material

Quantum Manipulation

Energy

Engineering at Microscale, for efficient energy exchange coherently

Life Sci.

quantum biology life process & quantum entanglement

> m num Information



Division of Quantum Physics & Quantum Information



















The Boson Experiment in Munich



Bare chamber (no magnetic coils, no optics, etc.)

- ⁸⁷Rb (bosons)
- $N_{BEC} \sim 10^5$
- T ~ 10nK
- 3D optical lattice $\lambda_z = 843$ nm $\lambda_{xs,ys} = 767$ nm
- **1D Superlattice** + $\lambda_{xl} = 1534$ nm
- Another Superlattice $+ \lambda_{yl} = 1534$ nm

















And a lot of optics and electronics !



Table 2





































- Adjusting ϕ by fine-tuning λ_{\prime}
- Offset-locking frequency-doubled fiber-laser to Ti:Sa-laser



• Offset-frequency $\Delta v = 1 - 2GHz$

→ Tuning range $\varphi = 0...2\pi$





• Novel state preparation techniques, e.g. patterned loading

$$\underbrace{}$$





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• Novel *read-out* methods, e.g. **sub-lattice resolved detection**



(Alternative: Raman-spectroscopy)





• Novel state read out techniques, e.g. Stern-Gerlach







• Atom pairs in long-lattice wells $|F = -1, m_F = 0\rangle$

• Initialize in
$$|F = I, m_F = 0\rangle$$

 Microwave-dressed spin-changing collisions

→ **Spin-pairs** in
$$|F = I, m_F = \pm I$$





A.Widera et al., PRL 95 (2005), F. Gerbier et al., PRA 73 (2006)



Preparing Entangled Spin Singlets

- Spin pairs in $|F = 1, m_F = \pm 1^{\circ} = |\uparrow \rangle, |\downarrow \rangle$
- Barrier raised slowly to split
 - Crossing a miniature Mott-transition: $n_{\text{Left}} = n_{\text{Right}}$

J. Sebby-Strabley et al., PRL 98 (2007)

• **Bosons**: Symmetric wavefunction \rightarrow Triplet $|t_0\rangle$ (Fermions: Antisymmetric wavefunction \rightarrow Singlet $|s_0\rangle$)

Details on the loading of the Spin-pairs: S. Trotzky et al., Science **319** (2008), A.-M. Rey at al., PRL **99** (2007)





2D Superlattice Geometries (2 SL)



Coupled Plaquette Systems

see B. Paredes & I. Bloch, PRA **77**, 23603 (2008) S. Trebst et al., PRL **96**, 250402 (2006)



Higher Lattice Orbital Physics

see V. Liu, A. Ho, C. Wu and others work exp: related to A. Hemmerich's exp.





- Isolated double-wells:
 - Correlated tunneling











- Isolated double-wells:
 - Correlated tunneling, Superexchange interactions









- Isolated double-wells:
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 - Counting atoms via interaction blockade











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 $|t_0\rangle$ $\frac{dB_x}{dx}$ **Triplet**: Singlet: B





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Non-equilibrium & adiabatic dynamics:

 Decay of patterned states (spin, density) after quantum quenches













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Isolated plaquettes:

- Resonating Valence Bond State
- Artificial Gauge Field
- Zak Phase in Topological Bloch Bands
- Many-body phases in the superlattice





CREATION OF STRONG EFFECTIVE MAGNETIC FIELDS

M. Aidelsburger *et al.*, PRL 107, 255301 (2011)



Quantum Hall effect in 2D electron gases

Integer quantum Hall effect





Artificial B fields with ultracold atoms

Rotation



The Coriolis force ${f F}_{
m C}=2m\,{f v} imes {f \Omega}_{
m rot}$ is analogous to the Lorentz force $\,{f F}_{
m L}=q\,{f v} imes {f B}$

Issue: typically $\gamma > 1000$

K. Madison *et al*, Phys. Rev. Lett. **84**, 806 (2000) J. R. Abo-Shaeer *et al*, Science **292**, 476 (2001)

Raman-induced gauge field



Spatially dependent optical couplings lead to a Berry phase analogous to the Aharonov-Bohm phase.

Issues: small *B* fields, heating from Raman lasers.

Y. Lin et al, Nature 462, 628 (2009)





Controlling atom tunneling along x with Raman lasers leads to effective tunnel couplings with spatially-dependent Peierls phases $\phi(\mathbf{R})$



Magnetic flux through a plaquette

$$\phi = \int_{\square} B \, \mathrm{d}S = \varphi_1 - \varphi_2$$

D. Jaksch & P. Zoller, NJP 5, 56 (2003) F. Gerbier & J. Dalibard, NJP 12, 033007 (2010) E. Mueller, PPA **70**, 041603 (2004)} A. Kolovsky, Europhys. Lett. 93, 20003 (2011)





Harper Hamiltonian: J=K and ϕ uniform.







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Quantum

Information

- Lowest band is topologically equivalent to lowest Landau level
- v=1/2 + repulsive interactions \longrightarrow Laughlin state for Bosons.

Consider a 2D optical lattice, where tunneling is inhibited along the x direction by a superlattice potential

D. Jaksch & P. Zoller, NJP 5, 56 (2003)
F. Gerbier & J. Dalibard, NJP 12, 033007 (2010)
A. Kolovsky, Europhys. Lett. 93, 20003 (2011)

Tunneling along this direction can be restored using Raman beams.

D. Jaksch & P. Zoller, NJP 5, 56 (2003)
F. Gerbier & J. Dalibard, NJP 12, 033007 (2010)
A. Kolovsky, Europhys. Lett. 93, 20003 (2011)

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- \rightarrow Staggered flux ϕ with zero mean
- → Tunable flux value, $\delta \mathbf{k} = \mathbf{k}_1 - \mathbf{k}_2$ (our setup: $\phi = \pi/2$)

$$K_{|ullet
angle
angle
angle
angle
angle
angle}(\mathbf{R}) = K \, e^{i\delta\mathbf{k}\cdot\mathbf{R}}, \quad K_{|\bigcirc
angle
angle
angle
angle}(\mathbf{R}') = K \, e^{-i\delta\mathbf{k}\cdot\mathbf{R}'}$$

Methods to rectify the flux:

- Linear potential gradient
- State-dependent lattices

D. Jaksch & P. Zoller, NJP 5, 56 (2003)

- F. Gerbier & J. Dalibard, NJP 12, 033007 (2010)
- A. Kolovsky, Europhys. Lett. 93, 20003 (2011)

In the limit of $V\kappa \ll \Delta$ the amplitude of the Raman-assisted tunneling is given by:

We load a ⁸⁷Rb condensate into a 2D-optical lattice.

 $\int \int \int \int J = 2\pi \times 60(3) \text{ Hz}$

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$$\bigvee_{x} \int_{x} \int_{x$$

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We switch on Raman lasers on resonance to induce tunneling.

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After 10 ms hold time, TOF images.

Reference: cubic lattice (no Raman drive)

J/K=1.0(1)

Due to the frustration introduced by the phase factors in $K(\mathbf{R})$, the condensation occurs for non-zero momenta.

Band structure

• 'Magnetic' Brillouin zone

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• Single-particle spectrum in the tight-binding approximation From the magnetic translation symmetries:

$$\psi_{|k_x,k_y\rangle}(\mathbf{R} = m \, \mathbf{d_x} + n \, \mathbf{d_y}) = e^{i(m \cdot k_x d_x + n \cdot k_y d_y)} \times \begin{cases} \psi_e & m \text{ even} \\ \psi_o \ e^{i \frac{\pi}{2}(m+n)} & m \text{ odd} \end{cases},$$

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An eigenstate $|k_x,k_y\rangle$ has two momentum components at (k_x,k_y) and $(k_x,k_y)+(k_s/2,k_s/2)$

Momentum distribution (J/K=1): comparison with theory

experiment

Momentum distribution (J/K=2.5)

experiment

The diffraction peaks are splitted \longrightarrow two-fold ground state degeneracy

Momentum distribution (J/K=2.5)

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G. Moeller, N. Cooper, PRA **82**, 1 (2010) J. Struck *et al.*, Science **333**, 996 (2011)

Momenta of the two degenerate ground states









Solution Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Control Contro







A lattice of plaquettes







State preparation for phase imprinting

• Load single atoms into ground state of tilted plaquettes:

$$|\psi_0\rangle = \frac{|A\rangle + |D\rangle}{\sqrt{2}}$$









State preparation for phase imprinting

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Information





State preparation for phase imprinting

• Load single atoms into ground state of tilted plaquettes:



• Switch on Raman coupling to induce atom transfer to the *B*, *C* sites In the limit *J*<<*K* the state is coupled to

$$|\psi_1\rangle = \frac{|B\rangle + i|C\rangle}{\sqrt{2}}$$



























Quantum 'Cyclotron' Orbit

 Classical: Charged particle in a uniform magnetic field







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• Measure quantum analogue: Initial state: Single atom in ground state of tilted plaquette







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Switch on Raman coupling to induce atom transfer



Site-resolved detection





Site-resolved detection







Site-resolved detection













Site-resolved detection









• Evaluate mean atom positions $\langle X\rangle$ and $\langle Y\rangle$





Cyclotron' Orbit

The mean atom position during the evolution.







Cyclotron' Orbit

The mean atom position during the evolution.















From this evolution we fit the value of the phase

$$\phi = 0.73(5) \pi/2$$

Deviation from $\phi = \pi/2$







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Using a linear potential

D. Jaksch & P. Zoller, NJP 5, 56 (2003)



Using a superlattice

F. Gerbier & J. Dalibard, NJP 12, 033007 (2010)







Using a linear potential D. Jaksch & P. Zoller, NJP **5**, 56 (2003) Using a superlattice + Gradient

F. Gerbier & J. Dalibard, NJP **12**, 033007 (2010)







Ladders in a magnetic field:

- ? Observables
- ? Edge current
- ? Bifurcation point
- ? Strong interaction
- ? Dirac point







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Detection of a vortex prepared in isolated 4-site plaquettes









Vacuum design—2D+MOT for K40







Vacuum design—Collimated Li6 atom beam

